

## Permutation from Swapping (1/4)

### • Recursive

- 1 + permutations of {2, 3, 4}
- 2 + permutations of {1, 3, 4}
- 3 + permutations of {2, 1, 4}
- 4 + permutations of {2, 3, 1}

1	2	3	4
1	2	4	3
1	3	2	4
1	3	4	2
1	4	3	2
1	4	2	3
2	1	3	4
2	1	4	3
...	...	...	...
3	2	1	4
3	2	4	1
...	...	...	...
4	2	3	1
4	2	1	3
...	...	...	...
4	1	2	3

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```
for (i=0; i<n; i++) a[i] = i+1;
permutation(a, 0, n-1);
```

1	2	3	4
1	2	4	3
1	3	2	4
1	3	4	2
1	4	3	2
1	4	2	3
2	1	3	4
2	1	4	3
...	...	...	...
3	2	1	4
3	2	4	1
...	...	...	...
4	2	3	1
4	2	1	3
...	...	...	...
4	1	2	3

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```
for (i=0; i<n; i++) a[i] = i+1;
permutation(a, 0, n-1);
```

```
void permutation(int perm[], int start, int end) {
    if (start == end) printPerm(perm, end+1);
    for (int i=start; i<=end; i++) {
        swap(&perm[start], &perm[i]);
        permutation(perm, start+1, end);
        swap(&perm[start], &perm[i]);
    }
}
```

1	2	3	4
1	2	4	3
1	3	2	4
1	3	4	2
1	4	3	2
1	4	2	3
2	1	3	4
2	1	4	3
...	...	...	...
3	2	1	4
3	2	4	1
...	...	...	...
4	2	3	1
4	2	1	3
...	...	...	...
4	1	2	3

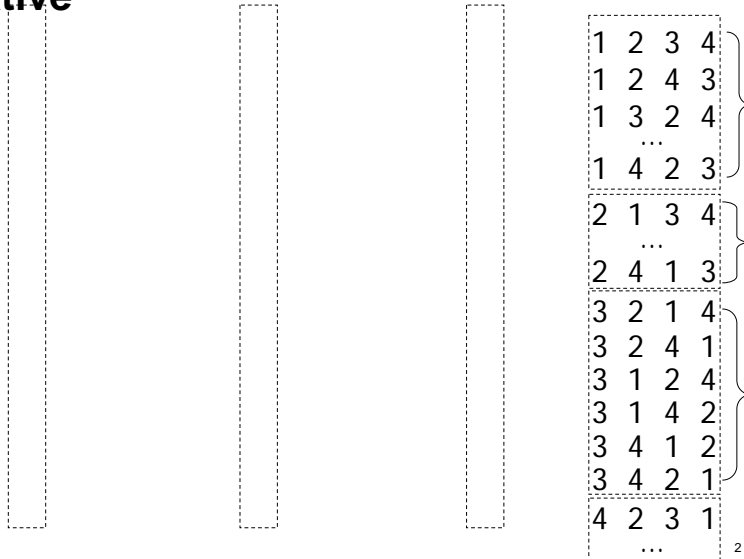
## Permutation from Swapping (2/4)

### • Iterative

1	2	3	4
1	2	4	3
1	3	2	4
...	...	...	...
1	4	2	3
2	1	3	4
...	...	...	...
2	4	1	3
3	2	1	4
3	2	4	1
3	1	2	4
3	1	4	2
3	4	1	2
3	4	2	1
4	2	3	1
...	...	...	...

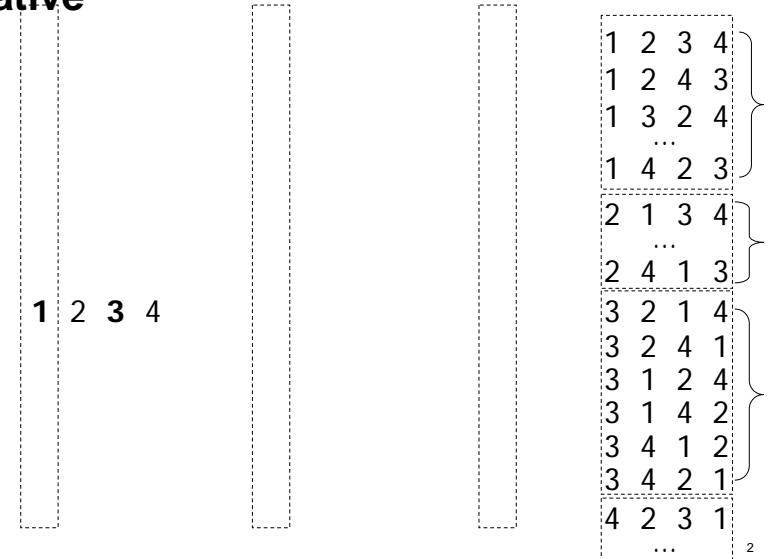
# Permutation from Swapping (2/4)

• Iterative



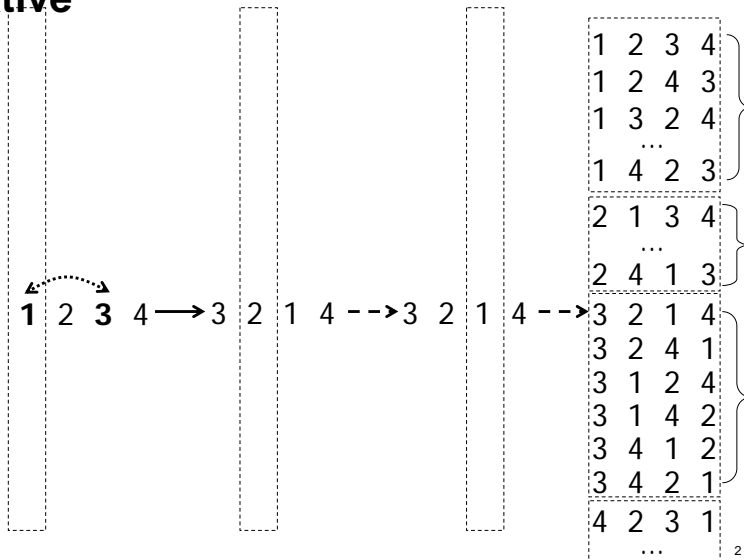
# Permutation from Swapping (2/4)

• Iterative



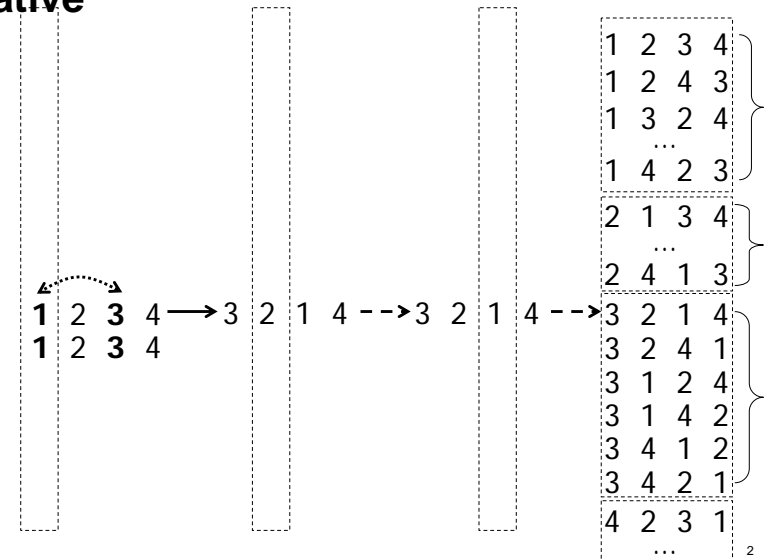
# Permutation from Swapping (2/4)

• Iterative



# Permutation from Swapping (2/4)

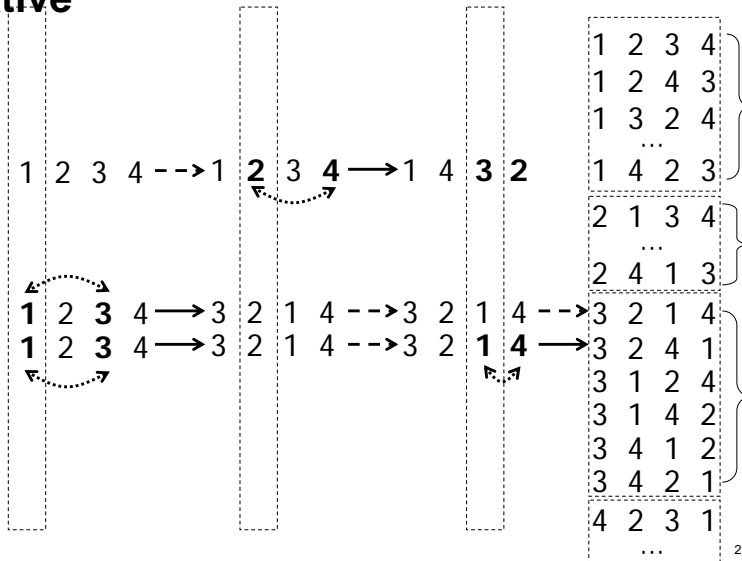
• Iterative





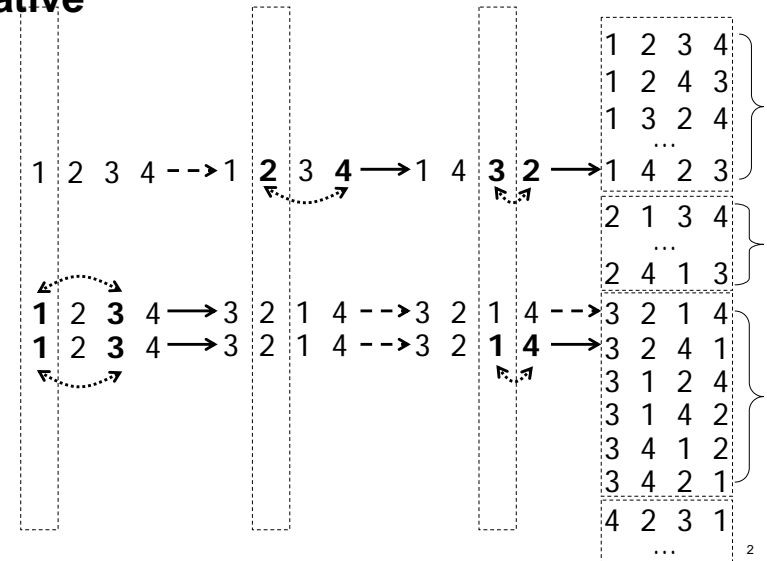
# Permutation from Swapping (2/4)

## • Iterative



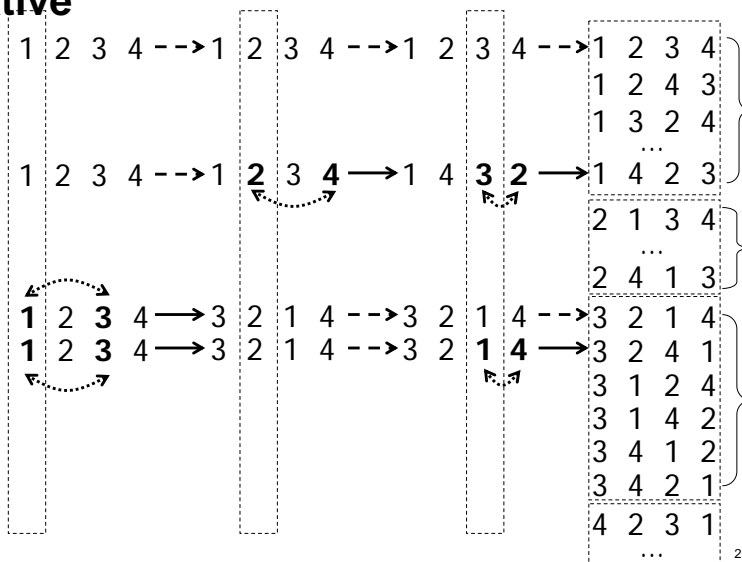
# Permutation from Swapping (2/4)

## • Iterative



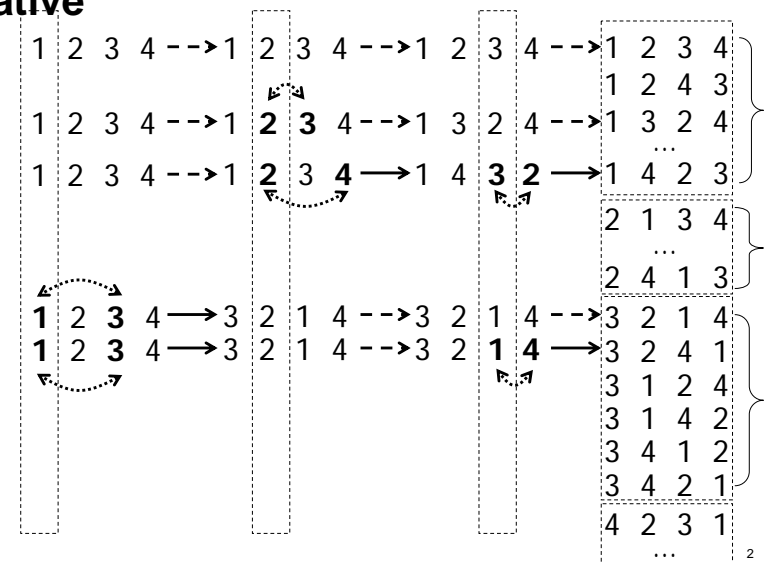
# Permutation from Swapping (2/4)

## • Iterative



# Permutation from Swapping (2/4)

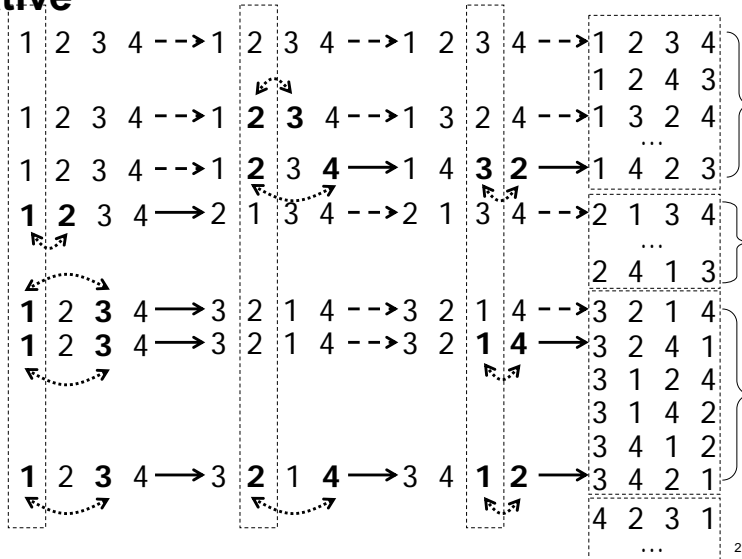
## • Iterative





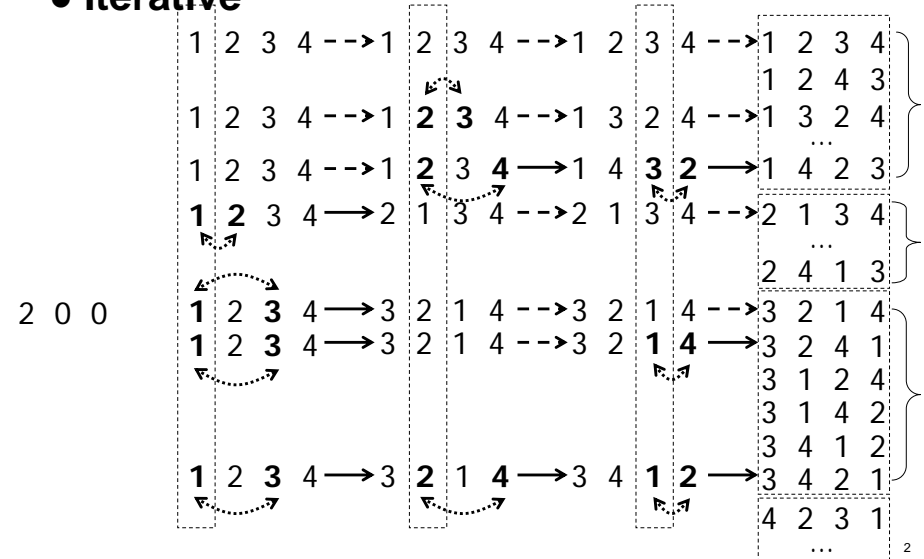
# Permutation from Swapping (2/4)

## • Iterative



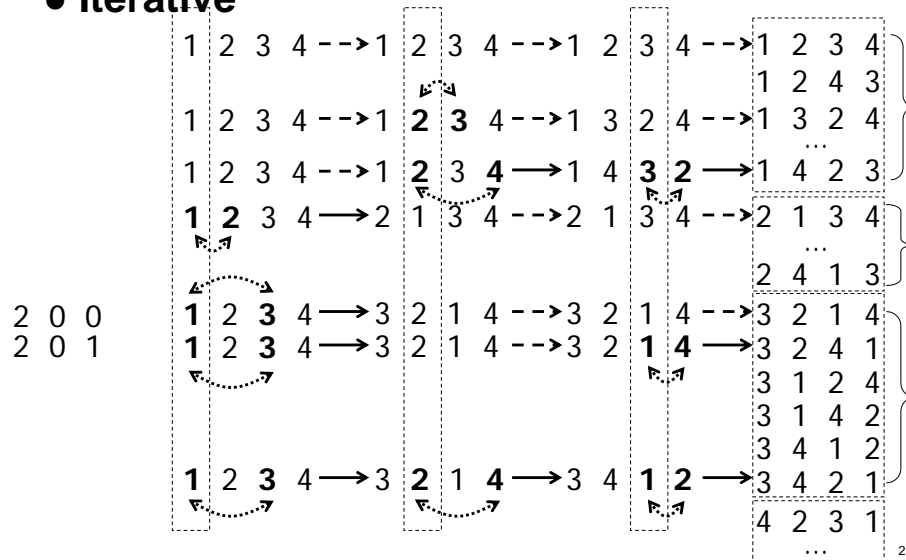
# Permutation from Swapping (2/4)

## • Iterative



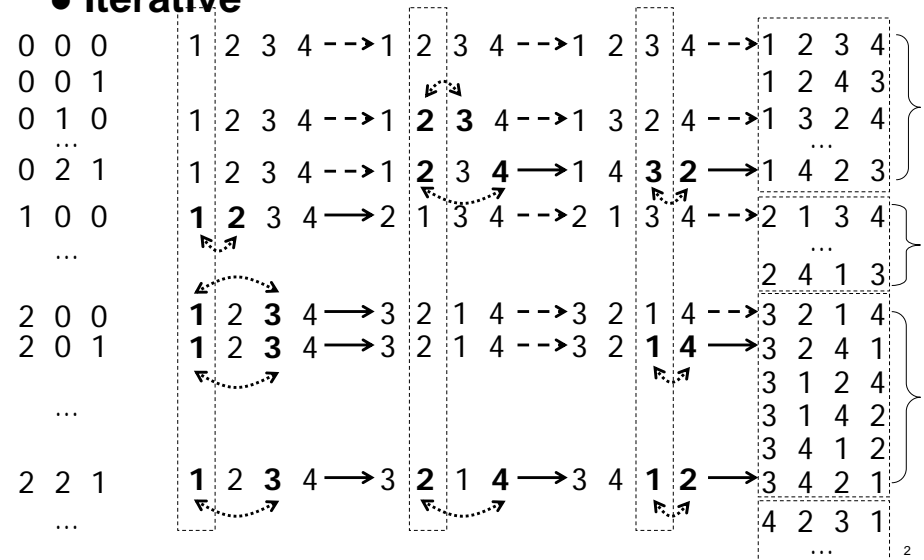
# Permutation from Swapping (2/4)

## • Iterative



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## • Iterative

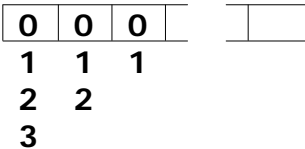


# Permutation from Swapping (3/4)

- counting up

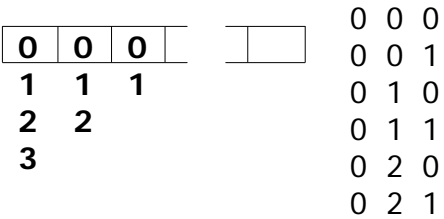
# Permutation from Swapping (3/4)

- counting up



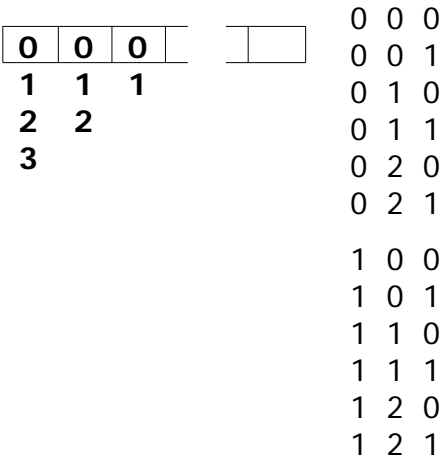
# Permutation from Swapping (3/4)

- counting up



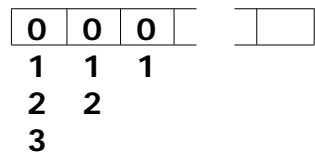
# Permutation from Swapping (3/4)

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# Permutation from Swapping (3/4)

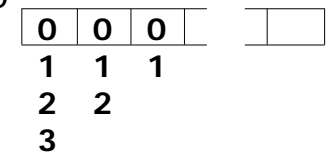
• counting up



0 0 0	2 0 0
0 0 1	2 0 1
0 1 0	2 1 0
0 1 1	2 1 1
0 2 0	2 2 0
0 2 1	2 2 1
1 0 0	
1 0 1	
1 1 0	
1 1 1	
1 2 0	
1 2 1	

# Permutation from Swapping (3/4)

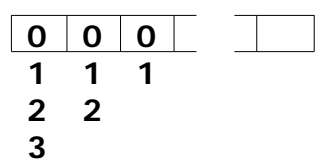
• counting up



0 0 0	2 0 0
0 0 1	2 0 1
0 1 0	2 1 0
0 1 1	2 1 1
0 2 0	2 2 0
0 2 1	2 2 1
1 0 0	3 0 0
1 0 1	3 0 1
1 1 0	3 1 0
1 1 1	3 1 1
1 2 0	3 2 0
1 2 1	3 2 1

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• counting up

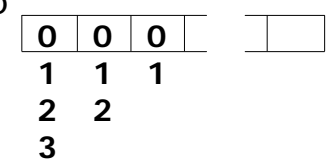


```
int next(int counter[], int size) {
    int i;
    for (i=size-1; i>=0; i--) {
        counter[i]++;
        if (counter[i]<=size-i)
            return 1;
        counter[i] = 0;
    }
    return 0;
}
```

0 0 0	2 0 0
0 0 1	2 0 1
0 1 0	2 1 0
0 1 1	2 1 1
0 2 0	2 2 0
0 2 1	2 2 1
1 0 0	3 0 0
1 0 1	3 0 1
1 1 0	3 1 0
1 1 1	3 1 1
1 2 0	3 2 0
1 2 1	3 2 1

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```
int next(int counter[], int size) {
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    for (i=size-1; i>=0; i--) {
        counter[i]++;
        if (counter[i]<=size-i)
            return 1;
        counter[i] = 0;
    }
    return 0;
}
```

0 0 0	2 0 0
0 0 1	2 0 1
0 1 0	2 1 0
0 1 1	2 1 1
0 2 0	2 2 0
0 2 1	2 2 1
1 0 0	3 0 0
1 0 1	3 0 1
1 1 0	3 1 0
1 1 1	3 1 1
1 2 0	3 2 0
1 2 1	3 2 1

Initially, 0 0 -1